

MONTGOMERY MODULAR MULTIPLIER USING A COMPRESSOR AND MULTIPLICATION METHOD

BACKGROUND OF THE INVENTION

[0001] This application claims priority from Korean Patent Application No. 10-2002-87243, filed on December 30, 2002, the entire contents of which are hereby incorporated by reference.

1. Field of the Invention

[0002] The present invention relates to a public-key cryptographic system, and more particularly, to a Montgomery modular multiplier.

2. Description of the Related Art

[0003] Cryptographic systems are used in communications achieved through smart cards, IC cards, and the like and have developed from secret-key cryptographic systems to public-key cryptographic systems. In a secret-key cryptographic system, two users must share an identical secret key in order to communicate with each other. Hence, key management and digital signing, which are based on a secret-key cryptographic system, are difficult. On the other hand, in a public-key cryptographic system, a secret key is secured by each user and any user who knows the public key of another party can communicate with that party, facilitating a process of convenient secret communications.

[0004] Examples of a public-key cryptographic system include Ron Rivest, Adi Shamir, and Len Adleman (RSA), Diffie-Hellman, a Digital Signature Algorithm (DSA), an Elliptic Curve Cryptosystem (ECC), and the like. Since a public-key cryptographic system performs modular multiplication to achieve a modular exponentiation operation, the system must adopt a modular multiplier.

[0005] A Montgomery modular multiplication algorithm, known as the most effective modular multiplication algorithm, can be expressed in pseudo code, as in Algorithm 1 below:

[Algorithm 1]

Stimulus:

$$A = (a_{n-1} a_{n-2} \dots a_1 a_0)_2, \text{ and } A < M$$

$$B = (b_{n-1} b_{n-2} \dots b_1 b_0)_2, \text{ and } B < M$$

$$M = (m_{n-1} m_{n-2} \dots m_1 m_0)_2, \text{ and } M \text{ is odd.}$$

Response:

$$S = (S_n S_{n-1} S_{n-2} \dots S_1 S_0)_2 \equiv ABR^{-1} \pmod{M}$$

Method:

$$S := 0$$

For i: = 0 to n-1 do

$$q_i := s_0 \text{ XOR } (b_i \text{ AND } a_0)$$

$$S := (S + b_i A + q_i M) / 2$$

endfor

[0006] That is, in Algorithm 1, a final S (sum) (in Algorithm 1, carry is expressed as S_n) that is calculated in a “for” loop is congruent to $ABR^{-1} \pmod{M}$. Here, “ R^{-1} ” is an inverse number of R modular-multiplied for “mod M”. When R is equal to 2^n , “ $(R \cdot R^{-1}) \pmod{M}$ ” is equal to 1.

[0007] The Montgomery modular multiplication algorithm performs only multiplications on given numbers A, B, and M, without using divisions, and is faster than other algorithms. Hence, the Montgomery modular multiplication algorithm is widely used in implementing public-key cryptographic systems, which require a modular exponentiation operation.

[0008] Conventional Montgomery modular multipliers based on a Montgomery modular multiplication algorithm are classified as a parallel multiplier, which uses a carry propagation adder as a basic accumulator, or a serial multiplier, which uses a 3-2 (3-input to 2-output) compressor (i.e., a carry save adder made up of full adders) as a basic accumulator.

[0009] A carry propagation adder requires a carry-propagation delay time on a clock-by-clock basis to propagate a carry upon every addition of multiple bits. Since the carry propagation adder cannot increase the carry-propagation delay time without limit, multiplication of numbers represented by 32 bits or more is difficult. In other words, the carry propagation adder has a larger power-delay product than in a carry save adder. The multiplication of a 32-bit number by a 32-bit number must be

repeated in order to perform a multiplication of numbers represented by 32 bits or more.

[0010] Since a serial multiplier that uses a carry save adder uses a 3-2 compressor (i.e., full adders), there are no problems of a propagation delay time, but the serial multiplier with the carry save adder is not easily implemented in hardware. The 3-2 compressor removes the propagation delay time by performing all additions on each bit at as many clock pulses as the number of bits. In other words, in a Montgomery modular multiplication algorithm such as Algorithm 1, the four words carry, S, b_iA , and q_iM must be summed. However, the 3-2 compressor can only receive 3 words, and accordingly, a problem arises in that the two main input words b_iA and q_iM need to be summed in advance. Also, when the 3-2 compressor performs addition, it must receive carry, S, and one of the four words (namely, carry, S, b_iA , and q_iM) and accordingly, requires a 4:1 multiplexer to select one of the four words.

SUMMARY OF THE INVENTION

[0011] Embodiments of the present invention provide a Montgomery modular multiplier that removes and/or reduces propagation delay time using a carry save adder (CSA) structure, in which all additions required for each bit are performed on four words (e.g., carry, S, b_iA , and q_iM), and additions in a carry propagation adder (CPA) structure are performed at an output stage, thereby achieving a fast operation speed and a small power-delay product.

[0012] Embodiments of the present invention also provide a Montgomery modular multiplication method in which a propagation delay time is removed and/or reduced using a carry save adder (CSA) structure, which performs all additions required for each bit on four words (e.g., carry, S, b_iA , and q_iM), and performs additions in a carry propagation adder (CPA) structure at an output stage, thereby achieving fast operation speed and a small power-delay product.

[0013] Another exemplary embodiment of the present invention, provides a Montgomery modular multiplier which calculates a value congruent to " ABR^{-1} " (mod M), where A and B are input n-bit numbers, R^{-1} is an inverse number of R modular-multiplied for "mod M", and M is a modulus. The Montgomery

modular multiplier includes an A-register, a B-register, an M-register, a b_iA calculation logic circuit, a q_i calculation logic circuit, a q_iM calculation logic circuit, a 4-2 compressor, an S-register, and a C-register.

[0014] The A-register stores a bit value a_i (where i is an integer ranging from 0 to $n-1$) of the number A , which is smaller than the modulus M .

[0015] The B-register stores a bit value b_i (where i is an integer ranging from 0 to $n-1$) of the number B , which is smaller than the modulus M .

[0016] The M-register stores a bit value m_i (where i is an integer ranging from 0 to $n-1$) of the modulus M , which is an odd number.

[0017] The b_iA calculation logic circuit multiplies the number A by a bit value b_i to obtain each bit of b_iA .

[0018] The q_i calculation logic circuit solves a Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ", where s_0 is the least significant bit (LSB) of a sum S , c_0 is the LSB of a carry C , b_i is the bit value of the number B , and a_0 is the LSB of the number A , to obtain a bit value q_i (where i denotes an integer in the range of 0 to $n-1$).

[0019] The q_iM calculation logic circuit multiplies the modulus M by the bit value q_i to obtain each bit of q_iM .

[0020] In an exemplary embodiment of the present invention the 4-2 compressor first performs n additions on the carry C , the sum S , the b_iA , and the q_iM to obtain interim values for each bit of the sum S and the carry C in a carry save adder structure and then sums the interim values to obtain final results of the S and C in a carry propagation adder structure, in response to a carry propagation adder signal.

[0021] The S-register updates a bit value s_i (where i is an integer ranging from 0 to $n-1$) of the sum S and stores the updated bit value.

[0022] The C-register updates a bit value c_i (where i is an integer ranging from 0 to $n-1$) of the carry C and stores the updated bit value.

[0023] In an exemplary embodiment of the present invention the 4-2 compressor includes a first full adder unit, a MUX unit, and a second full adder unit. The first full adder unit sums a bit value b_ia_i of the b_iA , a bit value s_{i+1} of the sum S , and the bit value c_i of the carry C to obtain a carry cA_i and a sum sA_i .

[0024] In an exemplary embodiment of the present invention the MUX unit selectively outputs either a bit value $q_i m_i$ of the $q_i M$, the carry $c A_{i-1}$, and the sum $s A_i$ or the bit value s_{i+1} of the sum S , the bit value c_i of the carry C , and the bit value c_{i-1} of the C , in response to the carry propagation adder signal.

[0025] The second full adder unit performs n additions on the bit value $q_i m_i$ of the $q_i M$, the carry $c A_{i-1}$, and the sum $s A_i$ to calculate interim bit values s_i and c_i of the sum S and the carry C , when the carry propagation adder signal is in an inactive state, and then sums the bit value s_{i+1} of the sum S , the bit value c_i of the carry C , and the bit value c_{i-1} of the carry C to obtain final results of the sum S and carry C , when the carry propagation adder signal is in an active state.

[0026] In an exemplary embodiment of the present invention the carry save adder structure is a 4-input 2-output structure, in which the first and second full adder units operate when the carry propagation adder signal is in an inactive state.

[0027] In an exemplary embodiment of the present invention the carry propagation adder structure is a 3-input 2-output structure, in which only the second full adder unit operates when the carry propagation adder signal is in an active state.

[0028] The LSB of the carry $c A_{i-1}$ and the LSB of the carry c_{i-1} are in a first logic state.

[0029] The MSB of the sum s_{i+1} is equal to the carry $c A_{n-1}$ at a clock pulse before the carry propagation adder signal is activated.

[0030] Another exemplary embodiment of the present invention, provides a method of performing a Montgomery modular multiplication in a Montgomery modular multiplier, which includes registers for storing bit values a_i , b_i , m_i , c_i , and s_i (where i denotes an integer in the range of 0 to $n*1$) of a word A , a word B , a modulus M , a carry C , and a sum S , respectively, and calculates a value congruent to " ABR^{-1} " (mod M), where A and B are input n -bit numbers, R^{-1} is an inverse number of R modular-multiplied for "mod M ", and M is a modulus. In the method, the number A , the number B , and the modulus M are received. The number A is multiplied by a bit value b_i to obtain each bit of $b_i A$. A Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ", where s_0 is the least significant bit (LSB) of a sum S , c_0 is the LSB of a carry C , b_i is the

bit value of the number B, and a_0 is the LSB of the number A, is obtained to obtain a bit value q_i (where i denotes an integer in the range of 0 to $n*1$). The number M is multiplied by the bit value q_i to obtain each bit of q_iM . Then, n additions are performed on the carry C, the sum S, the b_iA , and the q_iM to obtain interim values for each bit of the sum S and the carry C in a carry save adder structure, in response to a carry propagation adder signal. The interim values are summed to obtain the final results of the sum S and carry C in a carry propagation adder structure, in response to the carry propagation adder signal.

[0031] In an exemplary embodiment the number A is smaller than the modulus M.

[0032] In an exemplary embodiment the number B is smaller than the modulus M.

[0033] In an exemplary embodiment the modulus M is an odd number.

[0034] In an exemplary embodiment the interim and final values of the sum S and the interim and final values of the carry C are calculated by: summing a bit value b_iA_i of the b_iA , a bit value s_{i+1} of the sum S, and the bit value c_i of the carry C to obtain a carry cA_i and a sum sA_i ; selectively outputting either a bit value q_iM_i of the q_iM , the carry cA_{i-1} , and the sum sA_i or the bit value s_{i+1} of the sum S, the bit value c_i of the carry C, and a bit value c_{i-1} of the carry C, in response to the carry propagation adder signal; performing n additions on the bit value q_iM_i of the q_iM , the carry cA_{i-1} , and the sum sA_i to calculate interim bit values s_i and c_i of the sum S and the carry C, when the carry propagation adder signal is in an inactive state; and summing the bit value s_{i+1} of the sum S, the bit value c_i of the carry C, and the bit value c_{i-1} of the carry C to obtain final results of the sum S and carry C, when the carry propagation adder signal is in an active state.

[0035] In an exemplary embodiment the carry save adder structure is a 4-input 2-output structure, in which the interim values of the sum S and the carry C are obtained from the b_iA and q_iM when the carry propagation adder signal is in an inactive state. However the carry save adder can have a plurality of inputs and output structures.

[0036] The carry propagation adder structure is a 3-input 2-output structure, in which the final values of the sum S and the carry C are obtained from the

interim values of the sum S and the carry C when the carry propagation adder signal is in an active state. However the carry propagation adder can have a plurality of inputs and output structures.

[0037] The LSB of the carry cA_{i-1} and the LSB of the carry c_{i-1} are in a first logic state.

[0038] The MSB value of the sum s_{i+1} is equal to the bit value cA_{n-1} at a clock before the carry propagation adder signal is activated.

BRIEF DESCRIPTION OF THE DRAWINGS

[0039] The features of embodiments of the present invention will become more apparent from the detailed description and accompanying drawings, wherein:

[0040] FIG. 1 is a block diagram of a Montgomery modular multiplier according to an embodiment of the present invention;

FIG. 2 is a block diagram of the 4-2 compressor of FIG. 1 and its peripheral circuits in greater detail in an exemplary embodiment of the present invention;

FIG. 3 is a flowchart for illustrating the operation of the Montgomery modular multiplier according to an embodiment of the present invention in an exemplary embodiment of the present invention;

FIG. 4 is a block diagram for explaining the operation of a carry save adder in the Montgomery modular multiplier according to an embodiment of the present invention in an exemplary embodiment of the present invention; and

[0041] FIG. 5 is a block diagram for explaining the operation of a carry propagation adder in the Montgomery modular multiplier according to an exemplary embodiment of the present invention.

DETAILED DESCRIPTION OF EXEMPLARY EMBODIMENTS OF THE INVENTION

[0042] The following description of the exemplary embodiment(s) is merely exemplary in nature and is in no way intended to limit the invention, its application, or uses.

[0043] Embodiments of the present invention will now be described more fully with reference to the accompanying drawings, in which exemplary embodiments of the invention are shown. The embodiments of the present invention are provided in order to more completely explain the present invention to anyone skilled in the art.

[0044] Referring to FIG. 1, a Montgomery modular multiplier according to an embodiment of the present invention calculates a value congruent to " ABR^{-1} " (mod M). Here, A and B are input n-bit numbers, and R^{-1} is the inverse number of R modular-multiplied for "mod M." To accomplish this, the Montgomery modular multiplier includes an A-register 110, a B-register 120, an M-register 130, a b_iA calculation logic circuit 140, a q_i calculation logic circuit 150, a q_iM calculation logic circuit 160, a 4-2 compressor 170, an S-register 180, and a C-register 190.

[0045] The A-register 110 stores the bit value a_i (where i denotes an integer in the range of 0 to $n-1$) of the number A, which is smaller than the modulus M. The number A denotes a word representing an input n-bit number, and a_i is the value of each of the bits a_0 to a_{n-1} that constitute the number A.

[0046] The B-register 120 stores the bit value b_i (where i denotes an integer in the range of 0 to $n-1$) of the number B, which is smaller than the modulus M. The number B denotes a word representing an input n-bit number, and b_i is the value of each of the bits b_0 to b_{n-1} that constitute the number B.

[0047] The M-register 130 stores the bit value m_i (where i denotes an integer in the range of 0 to $n-1$) of the modulus M, which is an odd number. The modulus M denotes a word representing an input n-bit number, and m_i is the value of each of the bits m_0 to m_{n-1} that constitute the modulus M.

[0048] The b_iA calculation logic circuit 140 calculates each bit of b_iA by multiplying the number A by the bit value b_i . Consequently, the values of the n bits b_ia_0 to b_ia_{n-1} are output. At this time, since i varies from 0 to $n-1$ in the "for" loop included in Algorithm 1, the value b_i is obtained from the position of the least significant bit (LSB) of the B-register 120, which is right shifted by one bit every time an algorithm in the "for" loop is performed, as shown in FIG. 1.

[0049] The q_i calculation logic circuit 150 calculates the value q_i (where i denotes an integer in the range of 0 to $n-1$) used in the "for" loop of Algorithm

1 by solving the Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ". Here, s_0 is the LSB of a sum S , c_0 is the LSB of a carry C , b_i is a bit value of the number B , and a_0 is the LSB of the number A . At this time, since i varies from 0 to $n*1$ in the "for" loop included in Algorithm 1, a value b_i is obtained from the position of the LSB of the B-register 120, which is right shifted by one bit every time an algorithm in the "for" loop is performed, as shown in FIG. 1.

[0050] The q_iM calculation logic circuit 160 calculates each bit of q_iM by multiplying the modulus M by the bit value q_i . Consequently, the values of the n bits q_im_0 to q_im_{n-1} are output. At this time, since i varies from 0 to $n*1$ in the "for" loop included in Algorithm 1, i increases by one every time an algorithm in the "for" loop is performed, as shown in FIG. 1. Consequently, the values of the n bits q_0 to q_{n-1} are output.

[0051] In an exemplary embodiment of the present invention, in response to a carry propagation adder signal ONCPA, the 4-2 compressor 170 performs n additions on the C , the S , the b_iA , and the q_iM to obtain interim calculated values for each bit of the S and the C , in a carry save adder structure. Then, the 4-2 compressor 170 sums the interim calculated values to obtain the final results of the S and C , in a carry propagation adder structure. When the carry propagation adder signal ONCPA is in an inactive state, that is, is in a first logic state ("0"), first and second full adders operate at the same time in the carry save adder structure, thus forming a 4-input 2-output structure. When the carry propagation adder signal ONCPA is in an active state, that is, is in a second logic state ("1"), only the second full adders operate in the carry propagation adder structure, thus forming a 3-input 2-output structure.

[0052] The S-register 180 updates and stores the bit value s_i of the S (where i denotes an integer in the range of 0 to $n*1$). In other words, S denotes a word representing an n -bit number that is output as a sum, and s_i denotes the value of each of the bits s_0 to s_{n-1} that constitute the word S . The word S is updated every time an addition is performed in the carry save adder or carry propagation adder included in the 4-2 compressor 170.

[0053] The C-register 190 updates and stores the bit value c_i of the C (where i denotes an integer in the range of 0 to $n*1$). In other words, C denotes a word representing an n -bit number that is output as a carry, and c_i denotes the value of each of the bits c_0 to c_{n-1} that constitute the word C .

The word C is updated every time an addition is performed in the carry save adder or carry propagation adder included in the 4-2 compressor 170.

[0054] FIG. 2 is a block diagram of the 4-2 compressor 170 of FIG. 1 and its peripheral circuits in greater detail. Referring to FIG. 2, the 4-2 compressor 170 includes first and second full adder units 171 and 175 and a MUX unit 173, which form an adder with a 4-input 2-output structure.

[0055] Each of the first full adders of the first full adder unit 171 sums its corresponding bit value of the b_iA , the bit value s_{i+1} of the S, and the bit value c_i of the C to obtain a carry cA_i and a sum sA_i . The corresponding bit value of the b_iA is b_ia_i .

[0056] Each of the multiplexers in MUX unit 173 selectively output either its corresponding bit value of the q_iM , the carry cA_{i-1} , and the sum sA_i or the bit value s_{i+1} of the S, the bit value c_i of the C, and the bit value c_{i-1} of the C, in response to the carry propagation adder signal ONCPA. The corresponding bit value of the q_iM is q_im_i .

[0057] When the carry propagation adder signal ONCPA is in an inactive state, that is, in a first logic state "0", each of the second full adders of the second full adder unit 175 performs n additions on the bit value q_im_i of the q_iM , the carry cA_{i-1} , and the sum sA_i to calculate interim bit values s_i and c_i of the S and the C. When the carry propagation adder signal ONCPA is in an active state, that is, in a second logic state "1", each of the second full adders of the second full adder unit 175 sums the bit value s_{i+1} of the S, the bit value c_i of the C, and the bit value c_{i-1} of the C to obtain the final results of the S and C.

[0058] The carry cA_{i-1} denotes the carry of a bit that is one bit lower in position than the bit of the carry cA_i , which is output from the first full adder unit 171. The bit value s_{i+1} of the S denotes the sum of a bit that is one bit higher in position than the interim bit value s_i , which output from the second full adder unit 175. The bit value c_{i-1} of the C denotes the carry of a bit that is one bit lower in position than the bit value c_i , which is output from the second full adder unit 175.

[0059] As shown in FIG. 2, the LSBs of the carry cA_{i-1} and the carry c_{i-1} are in the first logic state, and the most significant bit (MSB) of the sum s_{i+1} is equal to the bit value cA_{n-1} at a clock pulse before the carry propagation adder

signal ONCPA is activated. The bit value cA_{n-1} is the MSB of the carry cA_i that is output from the first full adder unit 171.

[0060] The operation of the Montgomery modular multiplier according to an embodiment of the present invention of FIGS. 1 and 2 will now be described in detail with reference to FIG. 3.

[0061] The Montgomery modular multiplier according to an embodiment of the present invention includes registers, which store bit values a_i , b_i , m_i , c_i , and s_i (where i denotes an integer in the range of 0 to $n*1$) of a word A , a word B , a modulus M , a carry C , and a sum S , respectively, and calculates a value congruent to " ABR^{-1} " (mod M). Here, A and B are input n -bit numbers, and R^{-1} is an inverse number of R modular-multiplied for "mod A ".

[0062] In the operation of the Montgomery modular multiplier, first, the numbers A and B and the modulus M are received in step S311. In step S313, registers which store a parameter i and the sum S are reset to be 0 and initialized. The numbers A and B are smaller than the modulus M , and M is an odd number.

[0063] Thereafter, in step S315 to S319, the q_i calculation logic circuit 150 of the Montgomery modular multiplier obtains a value q_i (where i denotes an integer in the range of 0 to $n*1$) used in the "for" loop of Algorithm 1, by solving the Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ". Here, s_0 is the LSB of a sum S , c_0 is the LSB of a carry C , b_i is a bit value of the number B , and a_0 is the LSB of the number A . Also, in steps S315 to S319, the b_iA calculation logic circuit 140 multiplies the number A by the bit value b_i to obtain each bit of b_iA , and the q_iM calculation logic circuit 160 calculates each bit of q_iM by multiplying the modulus M by the bit value q_i . Also, in steps S315 to S319, the 4-2 compressor 170 performs n additions on the C , the S , the b_iA , and the q_iM to obtain interim values for each bit of the S and the C , in a carry save adder structure, which is formed when the carry propagation adder signal ONCPA is in an inactive state, that is, is in a first logic state ("0").

[0064] FIG. 4 is a block diagram for explaining the operation of a carry save adder in the Montgomery modular multiplier according to an embodiment of the present invention. Referring to FIGS. 3 and 4, in steps S315 to S317, each first full adder of the first full adder unit 171 sums its corresponding bit value of the b_iA , the bit value s_{i+1} of the S , and the bit value c_i of the C to

obtain a carry cA_i and a sum sA_i . Each second full adder of the second full adder unit 175 performs n additions on its corresponding bit value of the q_iM , the sum sA_i , and the carry cA_{i-1} , which are selected by the MUX unit 173, thereby calculating the interim values s_i and c_i of the sum S and the carry C .

[0065] As shown in FIG. 2, the bit output of the carry C is input to a first full adder corresponding to the bit, the bit output of the sum S is input to a first full adder corresponding to a bit that is one bit lower in position than the output bit, and a $1/2$ division operation included in the “for” loop of Algorithm 1 is performed, in step S315. The LSB of the carry cA_{i-1} is in the first logic state “0”. In other words, when the carry propagation adder signal ONCPA is in an inactive state, the 4-2 compressor 170 produces the carry save adder structure, which is a 4-input 2-output structure, and calculates the interim values of the S and C using the b_iA , and the q_iM .

[0066] After the interim values of the S and C are calculated for each bit, the carry propagation adder signal ONCPA is activated and enters in the second logic state “1”, in step S321. In steps S323 to S327, the 4-2 compressor 170 sums the calculated interim values of the S and C to obtain the final values of the S and C , in the carry propagation adder structure.

[0067] FIG. 5 is a block diagram for explaining the operation of the carry propagation adder in the Montgomery modular multiplier according to an embodiment of the present invention. Referring to FIGS. 3 and 5, in step S323, the second full adder unit 175 sums the bit value s_{i+1} of the S , the bit value c_i of the C , and the bit value c_{i-1} of the C , which are selected by the MUX unit 173, to calculate the final results of the S and C . As shown in FIG. 2, the MSB of the sum s_{i+1} is equal to the bit value cA_{n-1} at a clock before the carry propagation adder signal ONCPA is activated. The LSB of the carry c_{i-1} is in the first logic state “0”.

[0068] In step S325, the bit value s_{i+1} of the S , the bit value c_i of the C , and the bit value c_{i-1} of the C are summed for a period of time, (a propagation delay time for one bit)* (n bits), in the carry propagation adder structure. The propagation delay time for one bit consists of the propagation delay time of the second full adder unit 175 and the delay time of each of the 2:1 Muxes of the MUX unit 173. In other words, when the carry propagation adder signal ONCPA is in an active state, a 3-input 2-output carry propagation adder

structure is established, and the interim values of the S and C are summed in the 3-input 2-output structure to calculate the final values of the S and C.

[0069] As described above, the Montgomery modular multiplier according to an embodiment of the present invention includes registers, which store bit values a_i , b_i , m_i , c_i , and s_i (where i denotes an integer in the range of 0 to $n*1$) of a word A, a word B, a modulus M, a carry C, and a sum S, respectively, and calculates a value congruent to " ABR^{-1} " (mod M). Here, A and B are input n -bit numbers, and R^{-1} is an inverse number of R modular-multiplied for "mod A". The b_iA calculation logic circuit 140 calculates each bit of b_iA by multiplying the number A by the bit value b_i . At this time, the q_i calculation logic circuit 150 calculates a value q_i (where i denotes an integer in the range of 0 to $n*1$) by solving a Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ". Here, s_0 is the LSB of a sum S, c_0 is the LSB of a carry C, b_i is a bit value of the number B, and a_0 is the LSB of the number A. The q_iM calculation logic circuit 160 calculates each bit of q_iM by multiplying the modulus M by the bit value q_i . In response to the carry propagation adder signal ONCPA, the 4-2 compressor 170 performs n additions on the C, the S, the b_iA , and the q_iM to obtain interim calculated values for each bit of the S and the C, in a carry save adder structure. Then, the 4-2 compressor 170 sums the interim calculated values to obtain the final results of the S and C in a carry propagation adder structure. The final results of the S and C are output to the S- and C-registers 180 and 190, respectively.

[0070] As described above, the Montgomery modular multiplier according to an embodiment of the present invention removes propagation delay time by using a carry save adder (CSA) structure, in which all additions required for each bit are first performed on four words (e.g., C, S, b_iA , and q_iM), and then performs additions in a carry propagation adder (CPA) structure only at a final output stage. Hence, fast operation speed and a small power-delay product are achieved, thus improving the performance of a Montgomery modular multiplication algorithm.

[0071] Although embodiments of the present invention have been described with reference to various figures, the details of the figures should not be interpreted to limit the scope of the embodiments of the present invention. For example, figure 1 illustrates the use of a 4-2 compressor. The scope of

the present invention is not limited to a 4-2 compressor, various embodiments can use a plurality of input and output compressors. Likewise the scope of the embodiments of the present invention are not limited to three registers, A, M, and B. Other registers may be incorporated in combination with a compressor having a plurality of inputs and outputs. Further, the radix of the examples of the various embodiments are not limited to a particular radix value.

[0072] While exemplary embodiments of the present invention have been particularly shown and described, it will be understood by those of ordinary skill in the art that various changes in form and details may be made therein without departing from the spirit and scope of the present invention as defined by the following claims.